

# Verifiable Electronic Elections: Technical Solutions and Limits

*Rolf Haenni*

September 5th, 2014

*Im Zentrum der Sicherheitsanforderungen  
steht die Verifizierbarkeit.*

Bericht des Bundesrates zu Vote électronique  
Schweizerischer Bundesrat, 2013

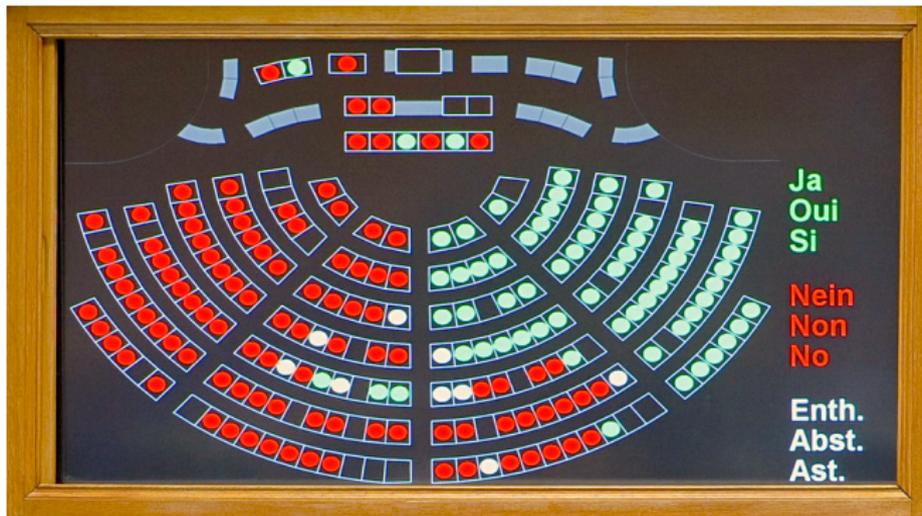
# Overview

- ▶ Introduction
- ▶ The Mathematics of Verifiable Elections
- ▶ Individual Verifiability
- ▶ Universal Verifiability
- ▶ Conclusion

# Introduction

*One should verify the election, not the election system.*

Ben Adida



# The Mathematics of Verifiable Elections

# Exponentiation

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Example:  $z = \text{Exp}(4) = 1$  for  $b = 2, n = 5$

# Very Large Numbers

If  $n$  and  $x$  are very large numbers ( $>300$  digits), for example

$n = 16193148119808063922021403359593144109458630491840281$   
 $35065105472372237877754754259914439249774193306631702$   
 $24569788019900180050114468430413908687329871251101280$   
 $87878658851566801277279829851162163414546460062661954$   
 $88232381853900348683549330501281156626636538418426995$   
 $35282987363300852550784188180264807606304297$   
(1024 Bits),

$x = \dots$

then

# Property 1: One-Way Function

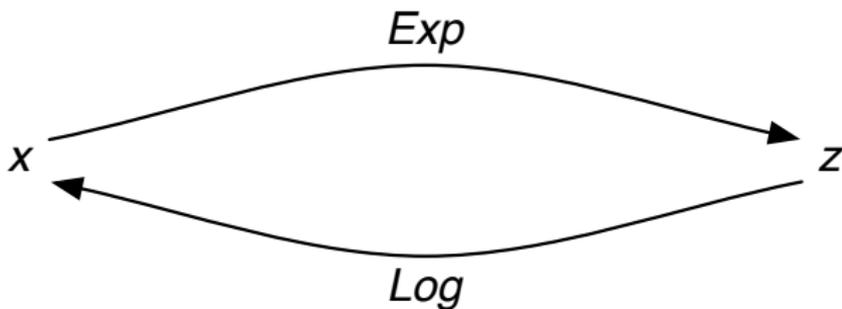
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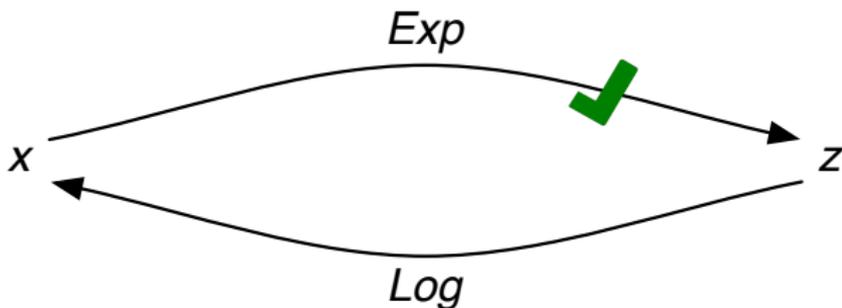
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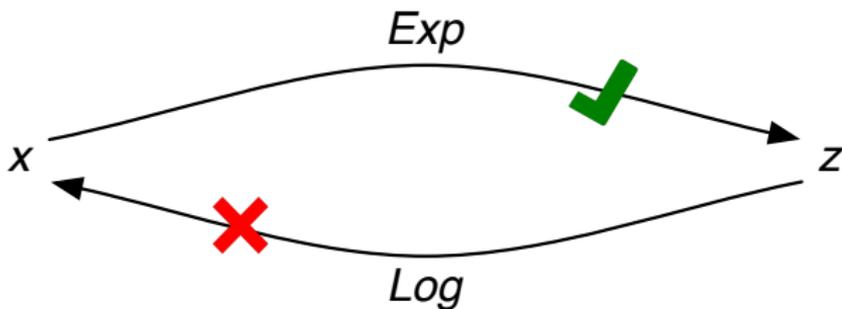
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# Zero-Knowledge Proofs

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- ▶ If I claim to know  $x$  such that  $z = \text{Exp}(x)$ , what can I do to make you believe me?

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- ▶ Option 1: Show you  $x$  and you check it
  
- ▶ Option 2: Compute a zero-knowledge proof
  - ▶ I give you a commitment  $t = \text{Exp}(r)$  for a random value  $r$
  - ▶ You give me a random challenge  $c$
  - ▶ I give you my response  $s = r + x \cdot c$
  - ▶ You check  $\text{Exp}(s) = t \cdot z^c$

# Applications in Electronic Voting

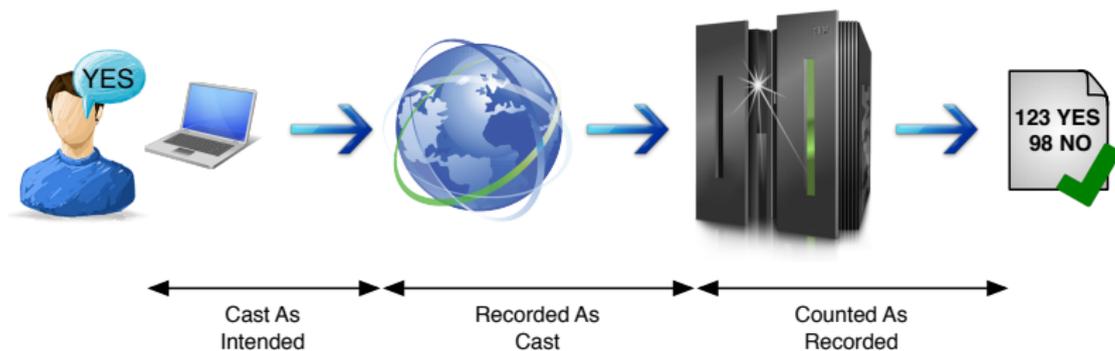
- ▶ Encrypting votes (ElGamal)
- ▶ Proving that an encrypted vote is either 0 or 1
- ▶ Summing up encrypted votes
- ▶ Computing verification codes from encrypted votes
- ▶ Re-encrypting an encrypted vote
- ▶ Shuffling a list of encrypted votes
- ▶ Proving that the re-encryption and shuffling was done correctly
- ▶ Sharing the decryption key
- ▶ Decrypting votes with shared keys
- ▶ etc.

# Individual Verifiability

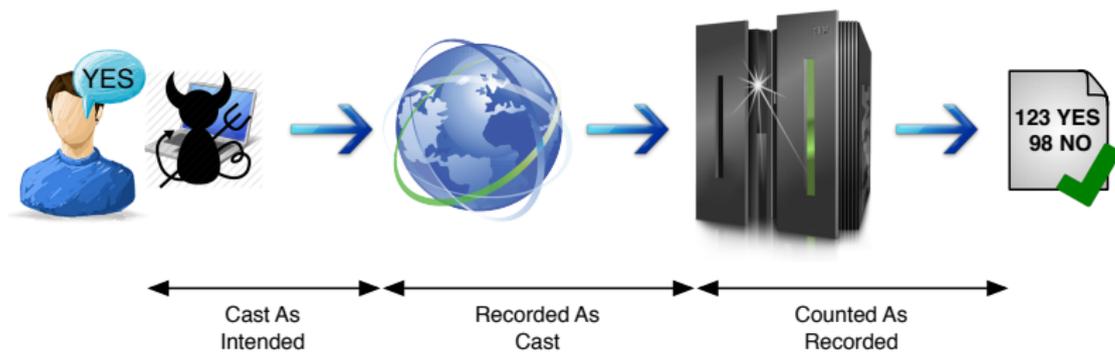
*Die Stimmenden müssen die Möglichkeit haben, zu erkennen, ob ihre Stimme auf der Benutzerplattform oder auf dem Übertragungsweg manipuliert worden ist.*

Verordnung der BK über die elektronische  
Stimmabgabe, VEleS, 2013

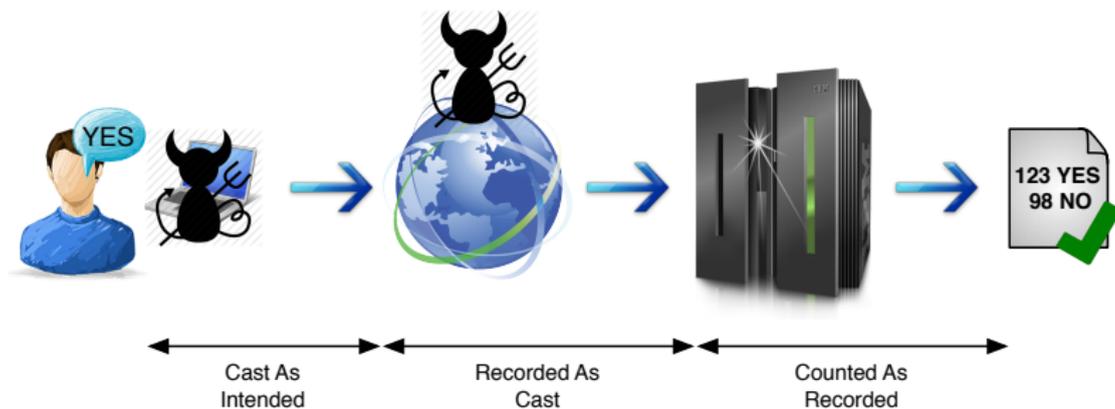
# Trust Model



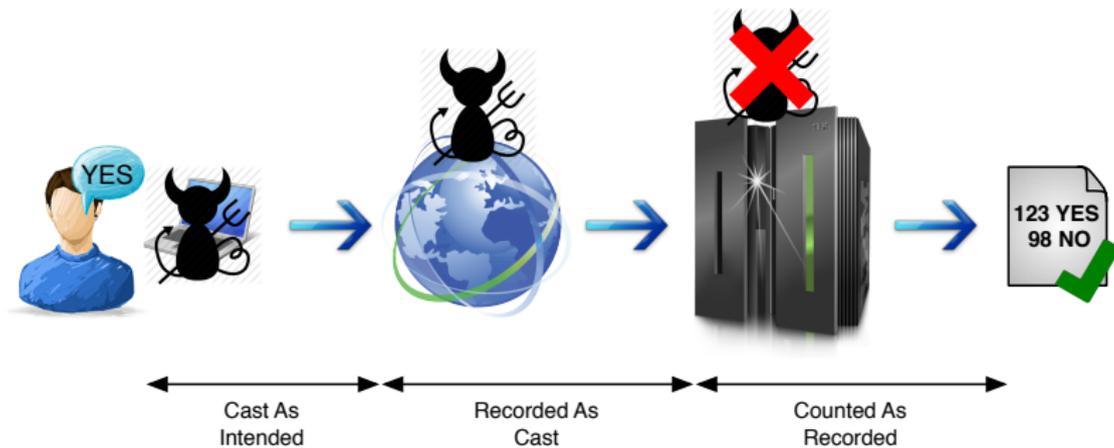
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- ▶ Verification codes are derived from the encrypted votes !

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# Individual Verifiability in Norway



R. E. Koenig, R. Haenni, and P. Locher.

Attacking the verification code mechanism in the Norwegian internet voting system. *VotID'13, 4th International Conference on E-Voting and Identity*, Guildford, U.K., 2013.

# Individual Verifiability in Switzerland

- ▶ The Norwegian verification mechanism can be adjusted to the “Swiss case”
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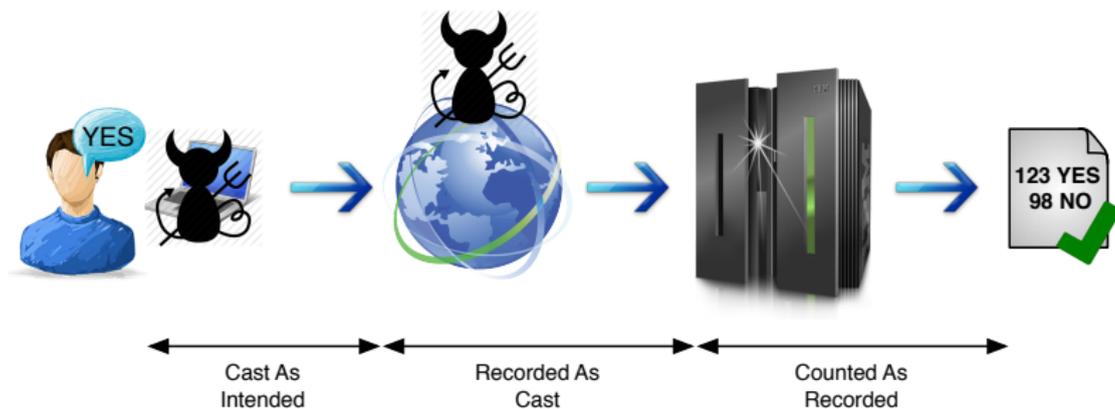
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# Universal Verifiability

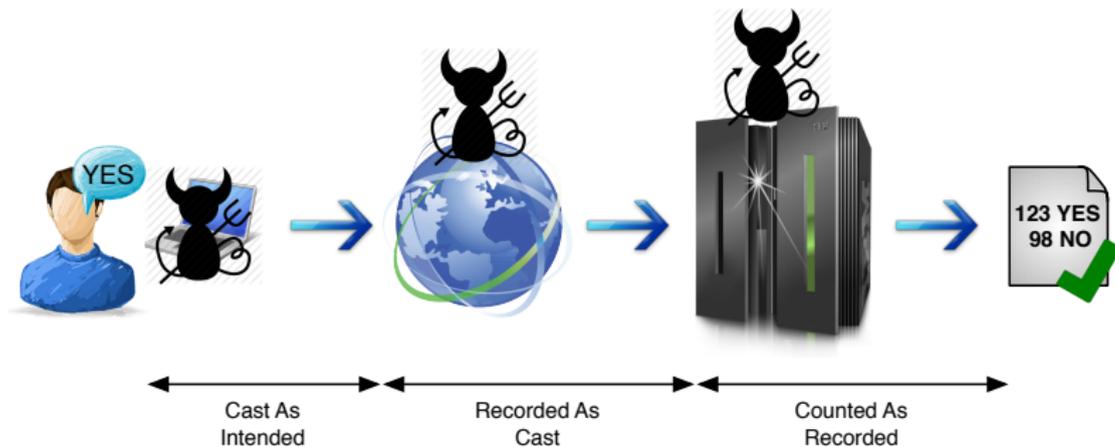
*Zur universellen Verifizierung erhalten die Prüferinnen und Prüfer einen Beweis der korrekten Ergebnisermittlung. [...] Dazu müssen sie technische Hilfsmittel verwenden, die vom Rest des Systems unabhängig und isoliert sind.*

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## VSBFH Studierendenratswahl 2014

Key Entry

**Vote**

Confirmation

Please prepare your vote by dragging the preferred list and candidates from the left column to the ballot on the right-hand-side. You can cast the ballot whenever you are ready.

### Candidates

List 1	+	SHEPPS	
List 2	+	---	
List 3	+	Kaufmann Claudia	Ⓜ +
List 4	+	Kaufmann Claudia	Ⓜ +
List 5	+	Dimitreijvic Jelena	Ⓜ +
List 6	+	Dimitreijvic Jelena	Ⓜ +
		Zurlinden Patrik	Ⓜ +
		Zurlinden Patrik	Ⓜ +
		Matter Celine	Ⓜ +
		Matter Celine	Ⓜ +
		Martin Lina	Ⓜ +
		Martin Lina	Ⓜ +
		Zimmermann Jessica	Ⓜ +

### Your Selection

List 4	↶ ↷ ⓧ
SHEPPS	---
Buri Samuel	Ⓜ ✖
Marwik Darius	Ⓜ ✖
Sommer Michael	Ⓜ ✖
Lüdi Marius	Ⓜ ✖
Schwendimann Adrian	Ⓜ ✖
Willi Benjamin	Ⓜ ✖
Käser Philip	Ⓜ ✖

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  - ▶ QR-code displayed on screen
  - ▶ They can copy/paste the image or take a snapshot

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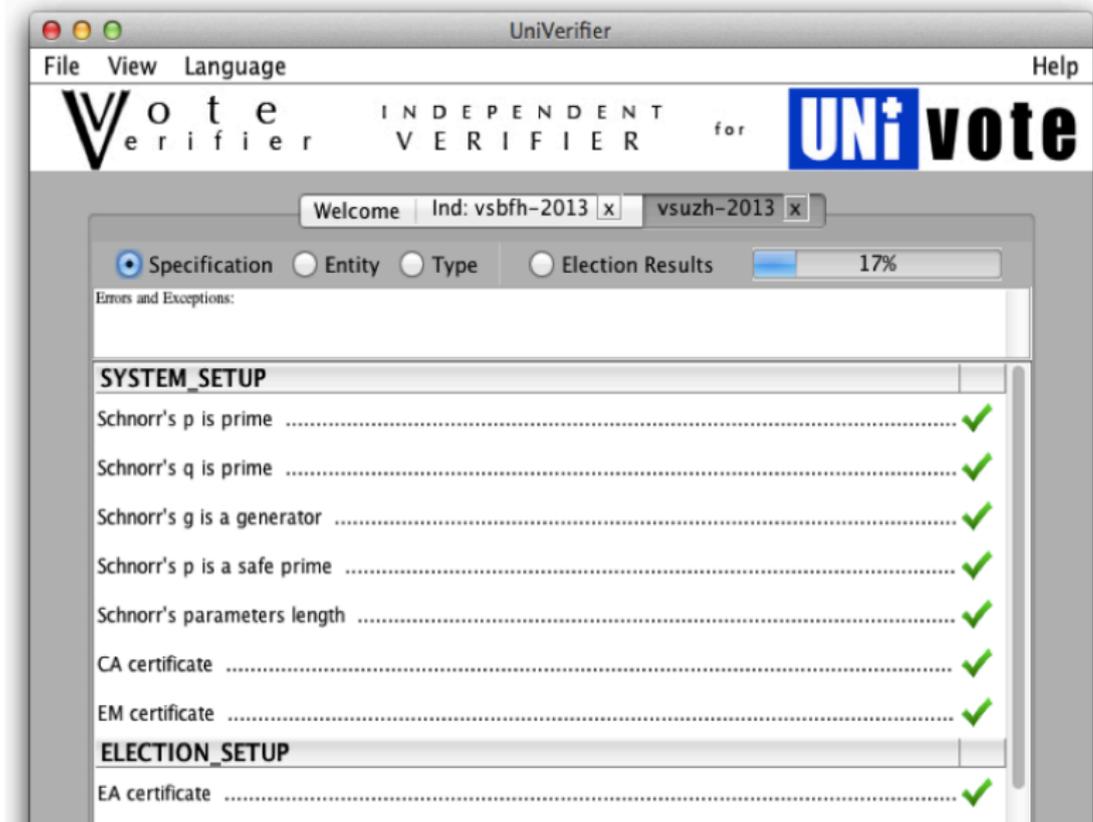
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- ▶ After the election, all voters can check
  - ▶ The inclusion of their votes (using the QR-code)
  - ▶ The correctness of the final result

# Universal Verifiability in UniVote

- ▶ The election data is published on the **public bulletin board**
  - ▶ System and election setup
  - ▶ List of candidates
  - ▶ List of voters and their voting keys
  - ▶ Anonymized list of voting keys (with zero-knowledge proof)
  - ▶ Encrypted votes (with zero-knowledge proofs)
  - ▶ Shuffled encrypted votes (with zero-knowledge proof)
  - ▶ Partial decryptions (with zero-knowledge proofs)
  - ▶ Decrypted votes
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  - ▶ Final result
- ▶ An independent software is needed to verify the election result



UniVerifier

File View Language Help

**V**oter **INDEPENDENT** **UNI**vote  
**er**ifier **VERIFIER** for

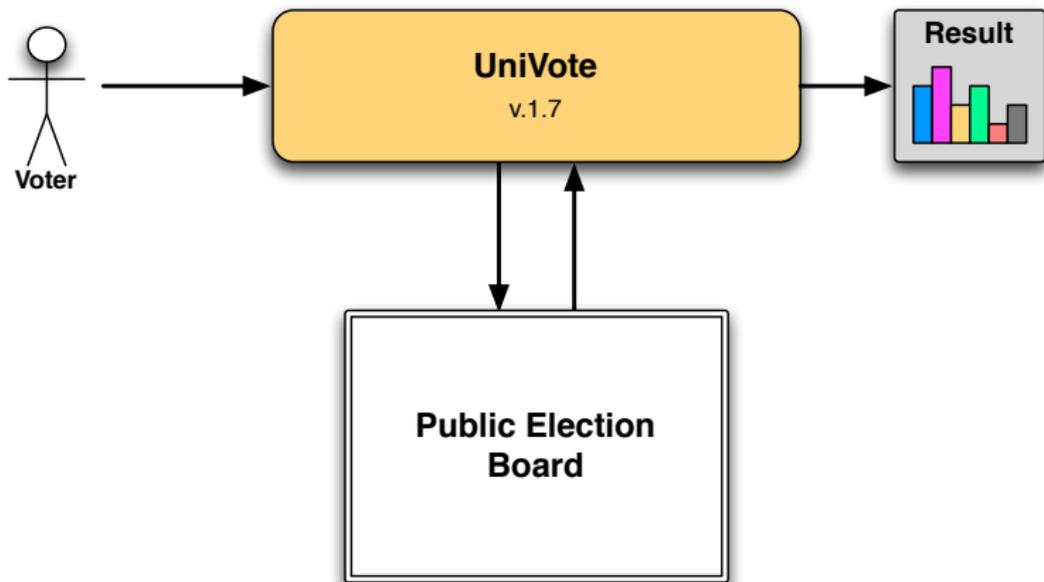
Welcome Ind: vsbfh-2013 x vsuzh-2013 x vsuzh-2013-1 x

Specification
  Entity
  Type
  Election Results
 40%

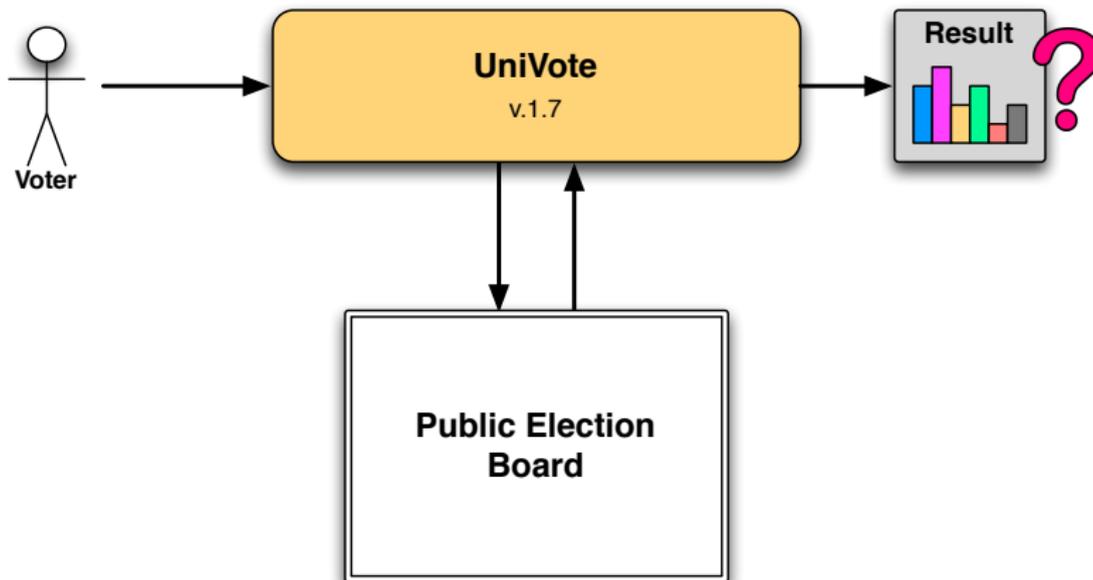
Errors and Exceptions:

<b>FVV</b>	<b>13</b>
1.1 Cornelia Vontobel	132
1.2 Saskia Keller	108
<b>IG Oerlikon</b>	<b>382</b>
2.1 Ivan Marijanovic	852
2.2 Roberto Ramphos	739
2.3 Muriel Ehrbar	775
2.4 Nadja Busch	756
2.5 Nina Egger	776
2.6 Tristan Jennings	727
2.7 Louis Binswanger	710

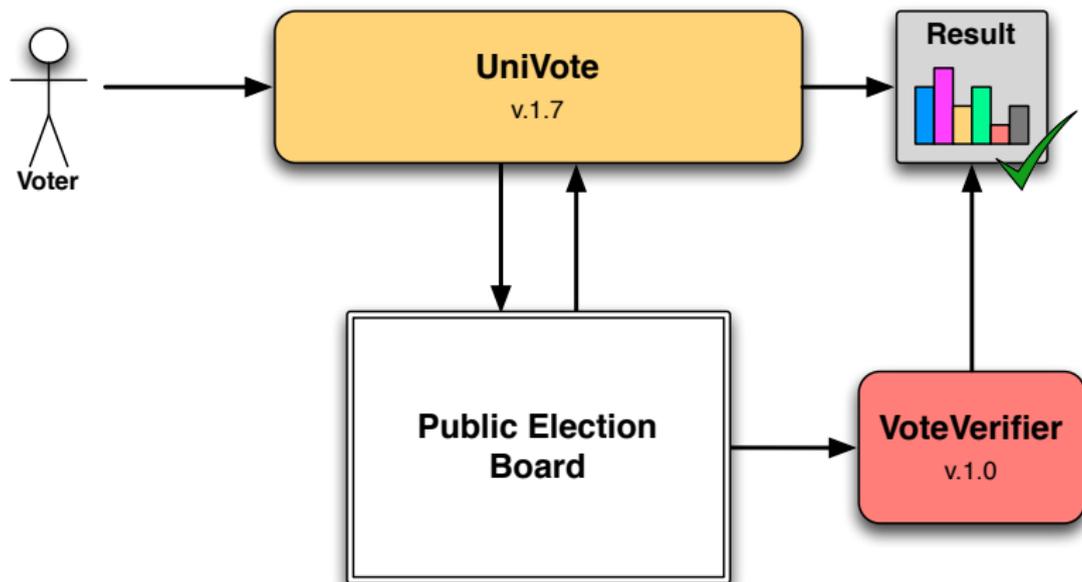
# Public Bulletin Board



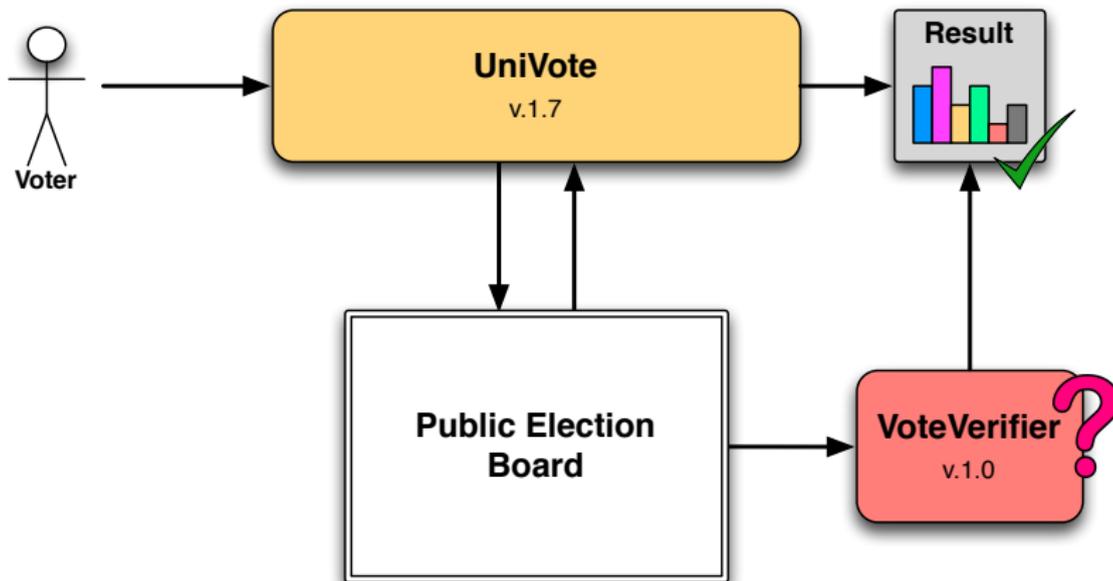
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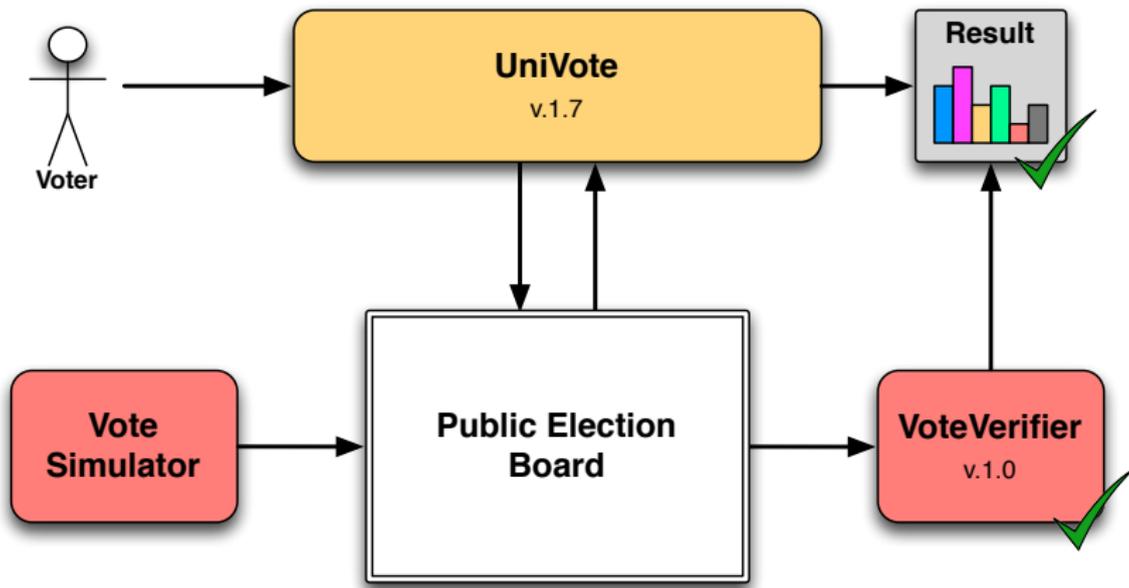
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- ▶ There are technical solutions and implementations
  - ▶ Individual verifiability: Norway
  - ▶ Universal verifiability: UniVote (and some others)
- ▶ Challenges
  - ▶ Complexity of some approaches
  - ▶ Cryptography in web browsers (JavaScript)
  - ▶ Usability and voter education
  - ▶ Vote secrecy on insecure platform
  - ▶ Voting buying and coercion

# VoteID 2015: The 5th International Conference on e-Voting and Identity

Home

Important Dates

Organization

Programme

Invited Speakers

Venue

Social Events

Accommodation

Registration

## VoteID 2015

September 2-4, 2015

Bern, Switzerland



More information about VoteID 2015 will be posted soon on this site. In case of questions, please e-mail to [info@voteid15.org](mailto:info@voteid15.org).

See

<http://www.voteid15.org>